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Title	Diversifying techniques and neutrality in genetic algorithms
Author(s)	Hill, Seamus; O'Riordan, Colm
Publication Date	2016
Publication Information	Hill, Seamus, & O'Riordan, Colm. (2016). Diversifying techniques and neutrality in genetic algorithms. Paper presented at the 8th International Conference on Evolutionary Computation Theory and Applications ECTA, Porto, Portugal, In Proceedings of the 8th International Joint Conference on Computational Intelligence - Volume 1: ECTA, (IJCCI 2016) ISBN 978-989-758-201-1, pages 140-147. DOI: 10.5220/0006036201400147
Publisher	SciTePress Digital Library
Link to publisher's version	https://dx.doi.org/10.5220/0006036201400147
Item record	http://hdl.handle.net/10379/14676
DOI	http://dx.doi.org/10.5220/0006036201400147

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Diversifying Techniques & Neutrality in Genetic Algorithms.

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Keywords: Neutral Theory, Genetic Drift, Neutrality, Genotype, Phenotype, Genetic Algorithms

Abstract: This paper examines the implicit maintenance of diversity within a population through the inclusion of a layered genotype-phenotype map (GP-map) in a Genetic Algorithm (GA), based on the principal of Neutral theory (Kimura, 1968). The paper compares a simple GA (SGA), incorporating a variety of diversifying techniques, to the multi-layered GA (MGA) as proposed by the authors. The MGA creates a neutral representation by including a layered GP-map based on the biological concepts of *Transcription* and *Translation*. In standard GAs, each phenotype is represented by a distinct genotype. However by allowing a higher number of alleles to encode phenotypic information on the genotype, one can create a situation where a number of genotypes may represent the same phenotype. Through this process one can introduce the idea of redundancy or neutrality into the representation. This representation allows for adaptive mutation (hot spots) and silent mutation (cold spots). This combination enables the level of diversity to dynamically adjust during the search, and directs the search towards closely related neutral sets. Previous work has shown that introducing this type of representation can be beneficial; in this paper we show how this representation is useful at introducing and maintaining diversity. Here we compare the performance of the MGA against traditional diversifying techniques used in conjunction with a SGA over a fully deceptive changing landscape.

1 INTRODUCTION

Genetic algorithms are search mechanisms based on Darwinian principals. However, simple genetic algorithms (SGA), through the representation used, implement a process of evolution without including the concept of neutral mutations. That is, representations in SGA do not adopt the notion of Neutral theory. Neutral theory can be described as a situation where the size of the search space is increased, without an equivalent increase in the solution space. This allows silent mutations to occur, where a mutated individual, at the genotypic level, can still represent the same phenotype. Kimura’s work indicated that the vast majority of mutations are caused by genetic drift rather than selection (Kimura, 1968). With this in mind, while natural selection is an important feature in the evolutionary process, only a fraction of DNA changes result in adaptation. This means that the majority of mutations taking place are phenotypically silent (Kimura, 1983). The motivation is to develop a tunable, synonymous, non-trivial GA representation which incorporates neutrality and to compare the implicit diversity created by the representation with that of a SGA, using a variety of diversifying techniques.

The contribution is to examine the use of a GA which is designed to implicitly maintain diversity within the population through its representation and to analyse the impact of the representation on population evolution. The paper is laid out as follows: Section 2 gives a brief background to Neutral theory and the use of neutrality in GAs. Section 3 outlines the genotype-phenotype map (GP-map) used in the paper, while Section 4 describes the experiments undertaken. Section 5 outlines and analyses the results and Section 6 concludes.

2 BACKGROUND

Previous research on the use of neutrality in evolutionary search produced mixed results. Smith et al. (Smith et al., 2001) highlighted the effect of neutral networks on the evolutionary search and concluded that neutrality does not provide an advantage. Ebner et al. (Ebner et al., 2001) examined the use of mutation and found that high levels of mutation could be sustained through the presence of neutral networks. They also identified that neutral networks assist in maintaining diversity in the population, which

could prove useful over changing landscapes. Similar results were also found in (Grefenstette and Cobb, 1993). Research carried out by Yu and Miller (Yu and Miller, 2001) illustrated that through the incorporation of neutrality, mutation may or may not be adaptive depending on the gene in question. They also examined neutrality using the OneMax problem, with results indicating that neutrality is advantageous as it allows the absorption of destructive mutations. Other research in the area includes (Hill and O’Riordan, 2105) which looked at the population dynamics of neutrality using a deceptive problem over a changing landscape. Results indicated that neutrality had a positive impact, allowing the search to escape local optima following the environmental changes. Problem difficulty also impacted on the usefulness of neutrality, as shown in (Hill and O’Riordan, 2104) and (Hill and O’Riordan, 2013).

3 GENOTYPE-PHENOTYPE MAPPING (GP-MAP)

In relation to redundancy, Information Theory provides a measurement of information. The information contained in a sequence, measured in *Bits* B , can be defined as the number of *bits* b required to represent that given information. In other words you need to be able to distinguish between the Bits, which represent the amount of information and the bits, which are used to represent the information (Rothlauf, 2002). If $b > B$, then your representation incorporates an element of redundancy. With regard to the multi-layered mapping of the MGA and using the notation outlined in (Rothlauf, 2002), as you progress through the layers, the level of redundancy alters. In the transcription layer, which maps $|\phi_g|$ (the genotype space) $\rightarrow |\phi_d|$ (the DNA space) $\rightarrow |\phi_r|$ (the RNA space), $k = 1$ (where k represents the order of the phenotypic building block) and there is no redundancy, therefore $b = B$ and $k_r = 1$ (where r can be defined as the number of genotypic building blocks of length kk_r used to represent a phenotypic building blocks of length k). In this paper, the chromosome length, $l_g = 24$ and $|\phi_g| = 2^{l_g}$. The DNA space $|\phi_d|$ consists of characters selected from a 4 character alphabet, with the DNA string $l_d = 12$ and $k = 3$. Therefore, $|\phi_d| = 4^{l_d}$ also $|\phi_d| = |\phi_r|$ and $l_d = l_r$ (the RNA string). The translation layer which maps $|\phi_r| \rightarrow |\phi_p|$ (the phenotype space), introduces redundancy into the mapping. In the translation layer, $b > B$, $r = 1$, $k_r = 3$ and $k = 1$. The RNA building blocks have size kk_r and the redundancy is uniform. As k represents the order of the phenotypic building blocks, there are 2^k different

phenotypes, which are represented by 4^{kk_r} different RNA strings. In other words, there are 4^{kk_r} different possibilities to encode a single phenotypic bit and $|\phi_p| = 2^{l_p}$. In this paper, the phenotype string $l_p = 4$. Although the redundancy is uniform, the Hamming distances are not minimal and therefore the redundancy is not linear.

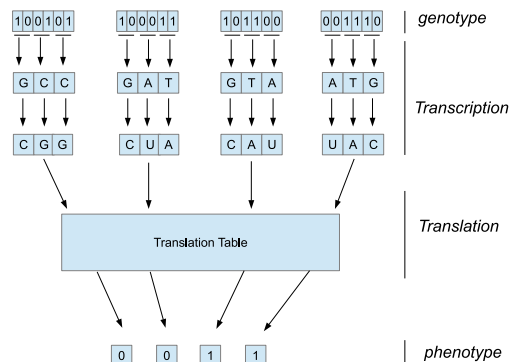


Figure 1: 6-bit MGA Representation Mapping

In summary, $|\phi_g| = \{0, 1\}^{l_g}$ where l_g is the genotype length. The transcription phase maps $|\phi_g| \rightarrow |\phi_d| \rightarrow |\phi_r|$. Where: $|\phi_d| = \{A, C, G, T\}^{l_g/2}$ with the following mappings: 00 \rightarrow A; 01 \rightarrow C; 10 \rightarrow G and 11 \rightarrow T. A bijective mapping maps $|\phi_d| \rightarrow |\phi_r|$, where: $|\phi_r| = \{A, C, G, U\}^{l_g/2}$. U is biologically inspired and has no impact on the evolution unless we include operators at this level. Following transcription, the translation phase takes place, mapping the RNA space to a phenotype space $|\phi_p|$, $|\phi_r| \rightarrow |\phi_p|$, where: $|\phi_p| = \{0, 1\}^{l_p}$, c is the cardinality chosen at initialisation to create a translation table, which maps 3 characters to a phenotype bit (either 0 or 1). The level of redundancy is determined by c , in this paper $c = 6$ (see Figure 1), and implies $|\phi_g| > |\phi_p|$ as $c > 1$. Missense mutation or substitution refers to a change in one amino acid in a protein, arising from a point mutation in a single nucleotide. Missense mutation in nature is carried out at the RNA level. In relation to the MGA, the Missense mutation mapping is as follows: $A \rightarrow U$, $C \rightarrow G$, $G \rightarrow A$ and $U \rightarrow C$. The variation operators, one-point crossover and single-point mutation occur at the genotype level prior to transcription and missense mutation takes place before translation. This mapping implicitly maintains related genetic diversity within the population, thus allowing the occupation by the population, of a greater number of neutral networks. This is possible as adaptive mutation occurs at c locations (hot zones) on the chromosome. The effect of this is to allow silent mutation to occur at $l_g - c$ locations (cold zones), which allows $2^{l_g - c}$ genotypes represent the same phenotype. This increases the level of diversity within the popu-

lation and allows the creation of neutral sets, which self-organise during evolution.

4 EXPERIMENT SET UP

Solutions and sub-solutions are normally lost in a SGA population for three reasons: *selection pressure*, *selection noise* and *operator disruption*. Selection pressure occurs as the result of the selection process, with less fit solutions disappearing from the population. Selection noise is the result of the variance of the selection process due to random choices between identically fit solutions. Operator disruption takes place through the implementation of the crossover and mutation operators which possess the ability to destroy good solutions. In an attempt to avoid premature convergence, techniques for diversifying a population generally attempt to reduce individually or in combination with one another, selection pressure, selection noise or operator disruption (Mahfoud, 1995).

Diversity within a population can serve a number of purposes, such as delaying convergence (note that premature convergence can be defined as the convergence to non-global optima) in order to promote exploration. Hence the maintenance of diversity within a population is a desirable feature for GAs. Diversification methods capable of reducing all three criteria, selection noise, selection pressure and operator disruption exist. The problem lies in the fact that reducing all three criteria to arbitrarily low levels results in the GA carrying out little or no useful search (Mahfoud, 1995). The maintenance of diversity for its own sake is undesirable; what is required is diversity that promotes good strings (Goldberg and Richardson, 1987).

By comparing the performance of the MGA with a SGA containing a number of diversifying techniques, we can evaluate the diversity maintenance mechanism implicit in the MGA representation. With regard to the three mechanisms for promoting diversity, the theory would suggest that Stochastic Universal Selection (SUS) offers the ability to minimise selection noise, fitness scaling can decrease selection pressure and lower rates of crossover and mutation can reduce operator disruption (Mahfoud, 1995). However it is worth remembering that a relationship exists between convergence and diversity in a GA population. If there is no operator disruption and no selection pressure, then the GA will maintain its initial population and won't perform any meaningful search. Also with regard the mutation operator, as mutation rates increase, the diversity produces is usually not useful

as the GA is approaching random search.

In this paper a four-bit changing deceptive landscape as outlined in (Hill and O'Riordan, 2105) was used. Although this landscape is relatively small in terms of the search space, it was chosen as it allows the dynamics of the population evolution to be studied. The parameters chosen are outlined in Table 1. Over the set of experiments designed to examine various diversifying techniques, we altered the selection mechanisms and scaling methods of the SGA. We also conducted a number of experiments where we increased the SGA's variation operators. The motivation for these changes is to vary the selection noise, selection pressure and operator disruption for the SGA, thereby examining the impact of the inclusion of well understood diversifying techniques into the SGA, which in turn are then compared with the performance of the MGA.

Parameters	MGA	SGA
Runs	10	10
Generations	200	200
Population P	20	20
Crossover P_c	0.7	0.7
Mutation P_m	$1/l$	$1/l$
Missense Mutation	0.2	No
Selection Mechanisms	Tournament	Various
Scaling Methods	No	Various

Table 1: Parameters Used

In Section 5 we outline the results of the experiments conducted. The selection noise experiments explore the use of Stochastic Remainder Selection (SRS) and SUS. The selection pressure experiments examine Linear, Window, Sigma Truncation and Boltzmann scaling techniques and niching techniques, such as, crowding and Incest Reduction. Finally, the operator disruption experiments look at the impact of increasing rates of crossover and mutation.

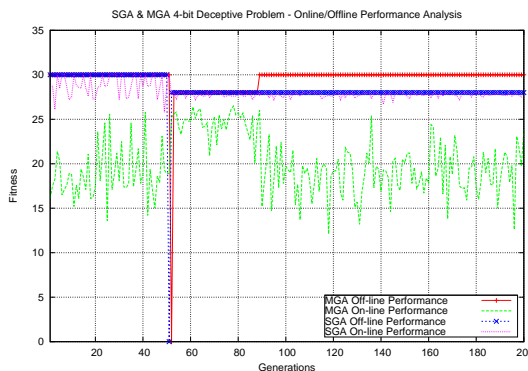


Figure 2: SGA & MGA On-line/Off-line

5 RESULTS

Figure 2 illustrates the off-line (averaged best fitness) and on-line (averaged fitness) performance for both the SGA and the MGA. The results indicate that the changing 4-bit deceptive landscape initially proved equally easy for both the SGA and the MGA, as they both located the global optimum. This is shown by the off-line performance of both GAs up to the change of landscape at generation 50. After the landscape changes, the SGA becomes trapped on the local optimum, while the MGA succeeds in locating the new global optimum. To analyse the results statistically, in this paper we used a Wilcoxon signed rank test to compare the off-line results of the SGA and MGA, and similarly to compare the on-line performances of both the SGA and MGA. The results indicated that the off-line results for both GAs were statistically significant with a $p\text{-value} < 2.2e^{-16}$. Similarly the on-line results were also statistically significant ($p\text{-value} < 2.2e^{-16}$).

5.1 Neutral Networks

The neutral networks representing various fitness values are shown in Figure 3. Before the landscape changes at generation 50, the most prominent neutral network represents the global optimum phenotype (1111). As the population evolves, the MGA, through its $M : 1$ representation, allows the size of neutral networks to adapt as the population evolves. The next largest neutral networks represent the phenotypes (0111), (1110), (1101) and (1011), which are the four genotypes closest in Hamming distance to the optimum, indicating that the MGA's population evolves towards neighbouring neutral sets.

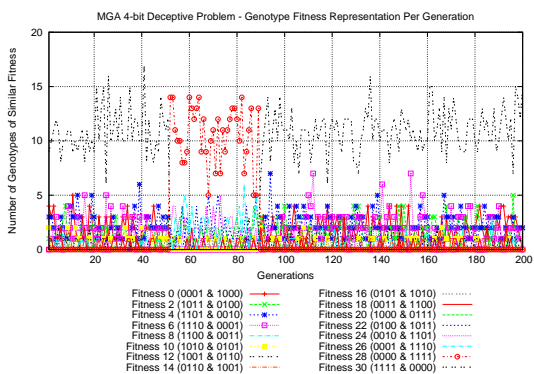


Figure 3: Neutral Networks - Number of Genotypes with Similar Fitness

As the landscape changes the largest neutral network represents the new local optimum (1111), as this was the global optimum at the time of the change.

As the search continues the MGA's population escapes the local optimum and has located the global optimum. At this point, the most prominent neutral network represents the phenotype (0000) (the new global optimum). Also, the MGA population has evolved towards a different group of neutral sets representing the phenotypes (0001), (0010), (0100) and (1000), all close, phenotypically, in Hamming distance to the global optimum.

Figure 4 looks at the composition of the neutral sets, examining the number of identical genotypes in each set. The figure indicates that there is a high degree of diversity maintained within each neutral set, with low numbers of identical genotypes present. The number of identical genotypes representing the global optimum varying between 2 and 4, illustrating the impact of the $M : 1$ representation on the population. Overall, the results indicate that the representation, implicitly maintains useful building blocks within the population, which promotes good strings and assist in improving the adaptability of the MGA.

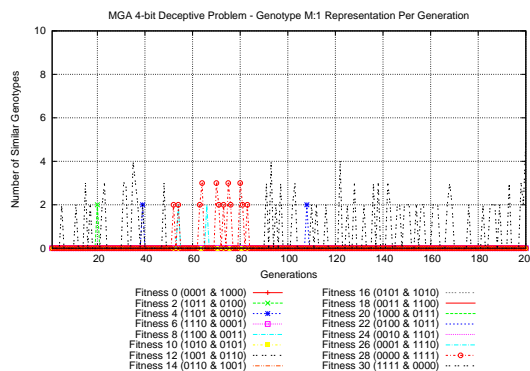


Figure 4: Neutral Networks - Identical Genotype

5.2 Selection Noise

As outlined by DeJong (De Jong, 1975), the variance of selection is one of the main contributors to the idea of convergence. In order to examine selection variance or selection noise, we compare a number of selection mechanisms designed to reduce selection noise, namely SRS and SUS. With SRS, the fitness of an individual f_i is divided by the average fitness of the population \bar{f} . For each string i where f_i/\bar{f} is greater than 1.0, the integer part of the number defines the number of copies of the individual are put forward for crossover. For example an individual with a fitness value of 1.45, places one copy forward for crossover and then has a 0.45 chance of putting a second copy forward.

SUS on the other hand, is optimal with respect to efficiency, bias (that is, the distance from the RWS in relation to expected value) and the spread (range

of possible individuals put forward for crossover) (Baker, 1985). SUS simulates a roulette wheel similar to RWS. However, while RWS spins the wheel n times ($n = \text{population size}$), SUS spins the wheel once, using n uniformly spaced pointers at the edge of the wheel. SUS has zero bias, is very efficient and minimises the spread and is regarded as the lowest noise selection scheme.

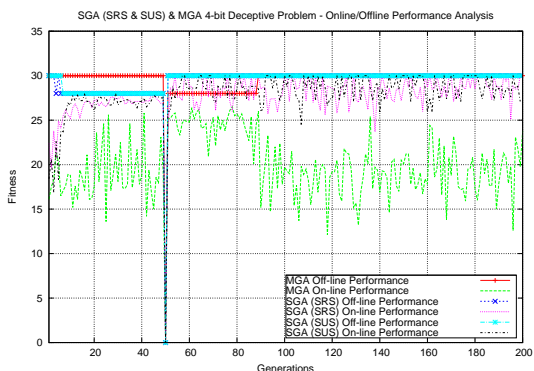


Figure 5: Selection Noise On-line/Off-line

Figure 5 indicates that the SGA (with SRS and SUS individually included), located the local optimum in the initial population, (see the off-line performances) due in part to the level of diversity (illustrated by the SGA on-line performance). However, the population converges prematurely as the search continues and diversity is quickly eliminated from the population. Once the landscape changes, because the population, for both the SRS and SUS SGAs, were trapped on the deceptive local optimum, they automatically located to new global optimum and remained there for the duration of the search. The MGA on the other hand located the global optimum both before and after the landscape change.

Off-Line	SRS	SUS	MGA
SRS	—	0.04131	0.09138
SUS	0.04131	—	0.4005
On-Line			
SRS	—	0.2732	$< 2.2e^{-16}$
SUS	0.2732	—	$< 2.2e^{-16}$

Table 2: Off-Line & On-Line Selection p-values

The statistical analysis of the results between the MGA and the SGA are shown in Table 2 and indicate that the off-line and on-line performance of SRS and SUS are quite similar to one-another. Comparing the MGA's off-line results to those of the SRS SGA, shows a less significant result than that of the off-line MGA and SUS SGA. The on-line performance of the MGA differs significantly from both of the SGAs.

Figure 6, illustrates the rate of convergence within the population and shows both the SGA (using SRS) and the SGA (using SUS) converging quickly. The

MGA maintains a higher degree of diversity, both at a phenotypic and genotypic level which assists in successfully locating the global optimum, both before and after the landscape change, as the level of diversity maintained allows the search to escape from the local optimum.

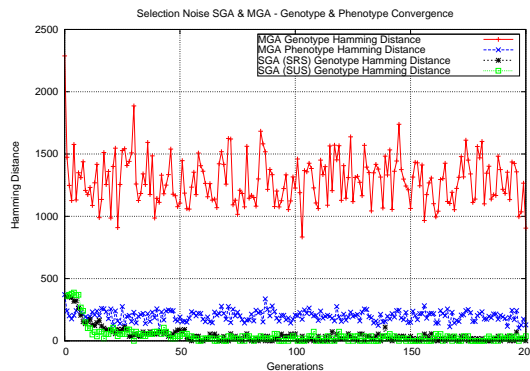


Figure 6: Selection Noise Convergence Rate

5.3 Selection Pressure

With selection, the extraordinary individuals within a population will begin to dominate the population quite quickly and premature convergence will begin to take hold. Even if there is significant diversity within a population, late in a run, the population's average fitness (on-line) may be close to the population's best fitness (off-line). This leads to a situation where the search for improvement becomes a "random-walk among the mediocre" (Goldberg, 1989).

5.3.1 Scaling Techniques

Fitness scaling has been used to overcome this problem. We now examine fitness scaling diversifying techniques aimed at reducing the selection pressure within the population:

- Linear scaling adjusts the fitness values of all individuals within the population, such that the fittest individual receives a fixed number of expected offspring and therefore prevents it from reproducing too frequently. The fitness function $f'_i = axf_i + b$ is used where a and b are normally selected so to allow the average individual receive, on average, one offspring copy, and the best receives the specified number of copies (normally two). This method may return a negative fitness value.
- Window scaling, fitness is scaled by subtracting from the raw fitness, the lowest fitness of any individual in the past number of scaling window

generations. The fitness function is $f'_i = f_i - f_w$, where w is the window size and is typically somewhere between 2 and 10 and f_w is the worst value observed in the w most recent generations.

- Sigma Truncation avoids returning negative fitness values for individuals within the population and incorporates problem dependant information into the scaling mechanism. The fitness of an individual f'_i is calculated as follows: $f'_i = f_i - (\bar{f} - cx\sigma)$, where c is a small integer value between 1 and 5, \bar{f} is the average raw fitness and σ is the population standard deviation. Negative values for f are avoided as any result $f < 0$ is set to zero. Individuals where $f_i < c$ standard deviation from the average fitness value are not selected.
- Boltzmann tournament selection procedure is derived and implemented to give stable distributions within a population. It also creates another niching mechanism for forming and sizing stable subpopulations of individuals according to differences among them, if the cooling process is not taken to the limit. Boltzmann scaling is expressed as $f' = e^{f_k/T}$ and selection pressure is low when the control parameter T is high.

The results of the scaling experiments are illustrated in Figure 7 and Table 3. These results indicate that the SGA using various scaling techniques, fails to maintain enough diversity within the population to avoid premature convergence. The statistical results indicate that differences between the various scaling methods, for these experiments, are minimal. The most significant results are between the MGA and the SGA using each of the scaling mechanisms. Figure 8, gives an overview of the rate of convergence associated with the SGA (incorporating scaling mechanisms) and the MGA. The graph illustrates that Linear, Window, Sigma Truncation and Boltzmann SGA loose diversity very quickly in the search, which results in the failure of the SGA to adapt after the landscape changes. The MGA implicitly maintains a level of diversity within the population which assists in adapting and locating the global optimum before and after the landscape change.

Off-Line	Linear	Window	Sigma T.	Boltzmann	MGA
Linear	—	1	0.5807	0.5716	$< 2.2e^{-16}$
Window	1	—	0.5807	0.5716	$< 2.2e^{-16}$
Sigma T.	0.5807	0.5807	—	1	$< 2.2e^{-16}$
Boltzmann	0.5716	0.5716	1	—	$< 2.2e^{-16}$
On-Line					
Linear	—	0.9319	0.1071	0.6711	$< 2.2e^{-16}$
Window	0.9319	—	0.04809	0.9433	$< 2.2e^{-16}$
Sigma T.	0.1071	0.04809	—	0.1353	$< 2.2e^{-16}$
Boltzmann	0.6711	0.9433	0.1353	—	$< 2.2e^{-16}$

Table 3: Off-Line & On-Line Scaling p-values

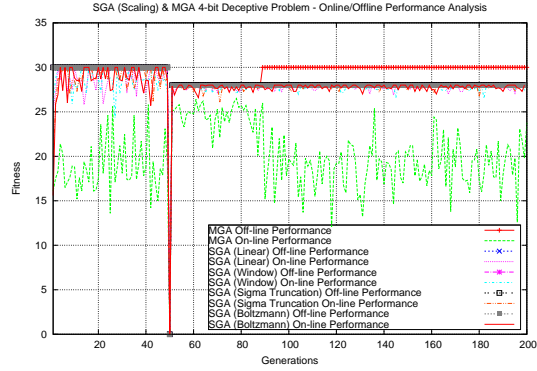


Figure 7: Selection Pressure On-line/Off-line

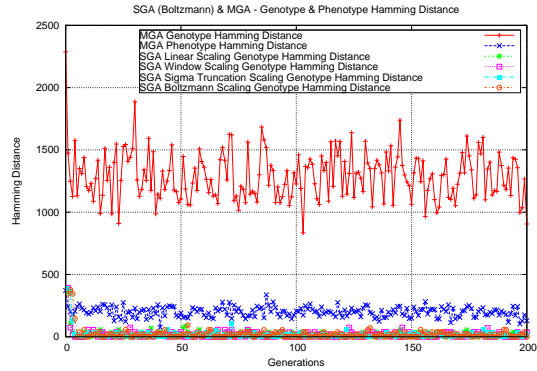


Figure 8: Selection Pressure Convergence Rate

5.3.2 Niching Techniques

Niching can be defined as an approach which encourages a number of distinct groups of genotypes to develop and remain in the population, with reduced pressure from the GA to converge towards a single type of genotype. Crowding involves a form of niching of the population. With crowding, as implemented in this paper, before crossover or mutation, normal fitness weighted selection is used to select members for the next generation. Crossover then takes place on individuals selected randomly from this set. After individuals have been selected for crossover, the offspring are created as usual. For each offspring, crowding factor, in this case 2, members of the survivors are selected randomly and the Hamming distance of each genotype from the offspring is calculated for 2 individuals. The offspring replaces whichever survivor is nearest in Hamming distance. Incest reduction is used in conjunction with crowding and introduces a mechanism to reduce the percentage of crossover between similar genotypes. After being selected, pairs are then selected for crossover by choosing the first parent at random from the list of selected individuals, then choosing a pre-defined (incest-reduction) number of possible candidates for the other parent randomly. The Hamming distance

of each candidate from the first parent and the one with the greatest Hamming distance is selected for crossover.

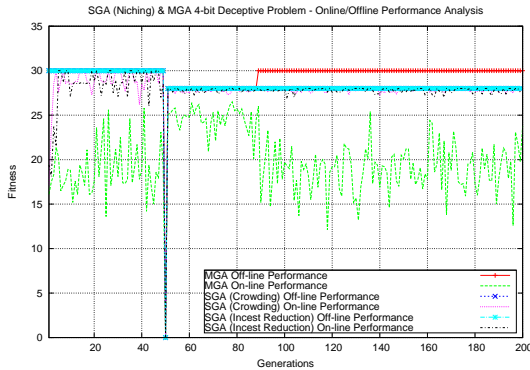


Figure 9: Niching On-line/Off-line

The results of the SGA performance with crowding and Incest reduction are shown in Figure 9. The results indicate that the performance of the SGA with crowding are very similar to those of the SGA incorporating Incest reduction (off-line p -value = 0.03351 and the on-line p -value = 0.1663). Both niching techniques fail to escape the local optimum. The MGA results differ, in that the diversity maintained within the population allows the search escape the deceptive trap. Comparing the MGA off-line and on-line results statistically against both of the niching techniques, indicated a high statistically significant difference in performance. In relation to the rate of convergence. Unlike the MGA, the niching techniques outlined, lose diversity early in the search (see Figure 10), making it difficult for the SGA to adapt and escape the local optimum when the environment changed.

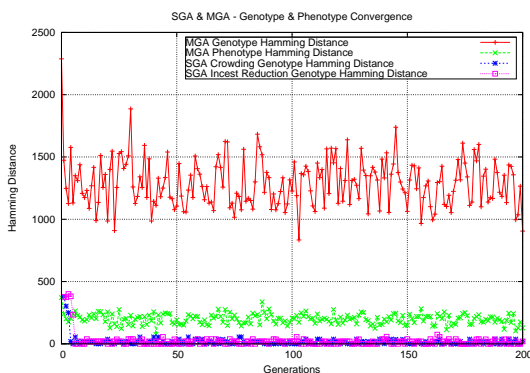


Figure 10: Niching Techniques Convergence Rate

5.4 Operator Disruption

For the operator disruption experiments, we increased the rate of P_c and P_m (see Figures 11 and 12 respectively). Examining the results of increasing the rate

of crossover to 0.90, the SGA located the global optimum early in the search but failed to adapt once the landscape changed. The results of increasing the rate of mutation to 0.50, illustrate that the search is being directed by randomness, with the SGA constantly moving to and from the global optimum, shown by the off-line performance. The result also shown a very large degree of change in the on-line performance. The increased crossover results, both off-line and on-line were significantly different from the MGA results (off-line p -value = $2.2e^{-16}$ and on-line p -value = 0.0003238). The results using mutation also indicated a statistically significant difference. The mutation off-line results indicate that increased mutation rates are statistically closer to the MGA results, however as the on-line results indicate, the search was driven by randomness and failed to produce good strings, meaning the diversity maintained wasn't useful in terms of a search algorithm.

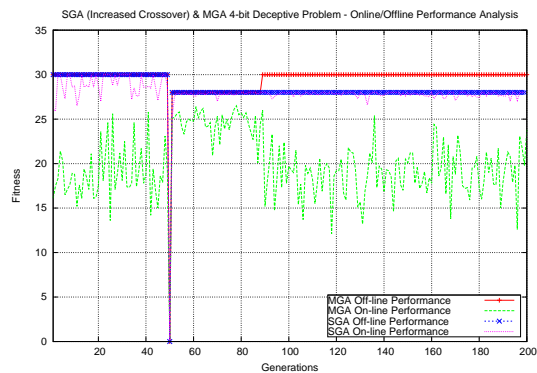


Figure 11: Operator Disruption (Crossover) On-line/Off-line

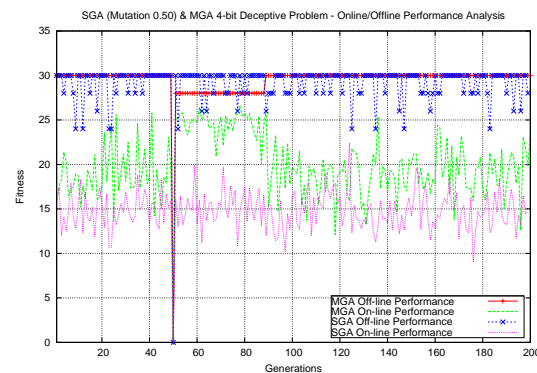


Figure 12: Operator Disruption (Mutation) On-line/Off-line

Regarding to the maintenance of diversity within the population, Figure 13 outlines the impact of operator disruption. Increasing crossover failed to maintain diversity within the population, which converged quickly. The mutation experiment increased the level of diversity within the population, but as mentioned

above, the search was directed by randomness. This random diversity failed to assist in the search.

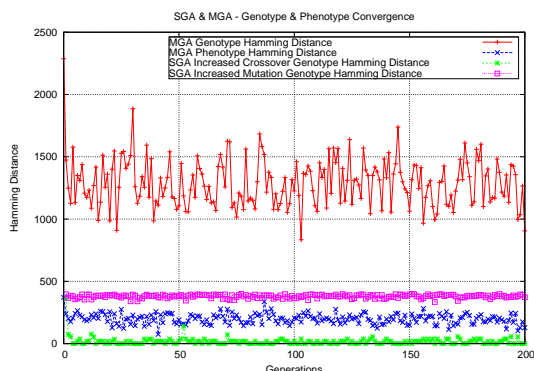


Figure 13: Operator Disruption Convergence Rate

6 CONCLUSION

The results presented, illustrate that through the implementation of Neutral theory, as proposed by Kimura (Kimura, 1968), the genotype-phenotype mapping of the MGA allows for a tunable, non-trivial, many-to-one relationship. By adopting this approach, convergence at a phenotypic level can be achieved, but genetic diversity is maintained at a genotypic level. Through the MGA's multi-layered genotype-phenotype mapping, adaptive (hot spots) and silent (cold spots) mutations become possible. This phenomenon allows neutral networks evolve within the population. The MGA, as a result of genetic drift, converges on neutral sets close to one another in Hamming space, which assists in relation to the adaptiveness of the MGA to changing environments. The results indicate that neutrality, as introduced by the MGA mapping, maintains a level of diversity within the population, which assists in searching dynamic landscapes as the diversity maintained by the MGA promotes good strings. When compared to a SGA incorporating a number of diversifying techniques, the implicit maintenance of diversity by the MGA proved successful in searching the deceptive dynamic landscape. The MGA, as a result of genetic drift, converges on neutral sets close to one another in Hamming space.

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